ORIGIN OF THE PROTON-TO-HELIUM RATIO ANOMALY IN COSMIC RAYS

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ABSTRACT

Recent data on Galactic cosmic rays (CRs) revealed that the helium energy spectrum is harder than the proton spectrum. The AMS experiment has now reported that the proton-to-helium ratio as function of rigidity $R$ (momentum-to-charge ratio) falls off steadily as $p/\text{He} \propto R^{-3}$, with $\Delta \approx -0.08$ between $R \approx 40 \text{GV}$ and $R \approx 2 \text{TV}$. Besides, the single spectra of proton and helium are found to progressively harden at $R \gtrsim 100 \text{GV}$. The $p/\text{He}$ anomaly is generally ascribed to particle-dependent acceleration mechanisms occurring in Galactic CR sources. However, this explanation poses a challenge to the known mechanisms of particle acceleration since they are believed to be “universal”, composition blind, rigidity mechanisms. Using the new AMS data, we show that the $p/\text{He}$ anomaly can be simply explained in terms of a two-component scenario where the GeV–TeV flux is ascribed to a hydrogen-rich source, possibly a nearby supernova remnant, characterized by a soft acceleration spectrum. This simple idea provides a common interpretation for the $p/\text{He}$ ratio and for the single spectra of proton and helium: both anomalies are explained by a flux transition between two components. The “universality” of particle acceleration in sources is not violated in this model. A distinctive signature of our scenario is the high-energy flattening of the $p/\text{He}$ ratio at multi-TeV energies, which is hinted at by existing data and will be resolutely tested by new space experiments ISS-CREAM and CALET.

Subject headings: cosmic rays — acceleration of particles — ISM: supernova remnants

1. INTRODUCTION: cosmic rays — acceleration of particles — ISM: supernova remnants

Precision data on proton and helium in Galactic cosmic rays (CRs) give important clues in understanding the origin of their energy spectrum. The leading theory is based on diffusive shock acceleration (DSA) mechanisms occurring in Galactic sources such as supernova remnants (SNRs, Blasi 2013; Bell 2014). In its linear and steady-state formulation, DSA predicts rigidity power-law spectra $\sim R^{-\nu}$ for all CR species, with $R \equiv p/Z$, and $\nu \approx 2.0$–2.1 for strong shocks. The acceleration spectra are expected to be further steepened to the observed spectra $E_{\gamma}$ (with $\gamma \approx 2.7$) by diffusive propagation of CRs in the interstellar medium (ISM). In the several models that are based on this picture (Grenier et al. 2015), the CR flux is generally assumed to arise from the contribution of a large population of SNRs, continuously distributed on the Galactic disk and time-averaged for their histories. In these models, the key source parameters such as spectral indices $\nu$ and elemental composition are therefore seen as effective quantities, determined from the data, representing the average SNR properties. While there is no doubt that SNRs are capable of non-thermal acceleration, there are many open questions about the details of the DSA mechanism and its time dependence. Which types of SNRs make up the CR flux observed at Earth? At which stage of the evolution of an SNR is the CR spectrum is released in the ISM?

Puzzling features recently found in the CR spectrum may offer an opportunity to shed light on these open questions (Maestro 2015; Serpico 2015). Here, we focus on the so-called proton-to-helium ($p/\text{He}$) anomaly, i.e., the unexplained spectral difference between protons and helium. Recent data from PAMELA, BESS, and AMS reported that the $p/\text{He}$ ratio as function of rigidity decreases steadily as $R^{-\Delta}$ (Adriani et al. 2011; Abe et al. 2015; Aguilar et al. 2015b). In particular, AMS measured $\Delta \approx -0.08$, at rigidity $R = 45$–1800 GV. This anomaly poses a serious challenge to acceleration models based on the DSA theory. Known DSA mechanisms are “universal” processes of rigidity (or gyroradius), i.e., they predict elemental-independent spectra at relativistic energy (Schwarzchild 2011; Serpico 2015). It was proposed that the He spectrum may harden due to spallation, which has a particle-dependent timescale, in competition with the diffusion timescale (Blasi & Amato 2011) or in models with re-acceleration on weak shocks (Ptuskin et al. 2013; Thoudam & Horandel 2014). However, for reasonable values of cross sections and gas density, the spallation effect is expected to be ineffective on the $p/\text{He}$ ratio above a few $\sim 10$ GV of rigidity (Putze et al. 2011; Vladimirov et al. 2012). Moreover, the He spallation is dominated by the reaction $^4\text{He} + p \rightarrow ^3\text{He} + X$, which does not harden the total He spectrum (Vladimirov et al. 2012). A detailed study in Vladimirov et al. (2012) concluded that the $p/\text{He}$ data are best reproduced if the spectral difference is ascribed to acceleration. This is de facto a standard assumption of recent CR propagation models, where the source functions $q(R) \propto R^{-\nu}$ make use of elemental-dependent spectral indices $\nu = \nu(Z)$. Specific mechanisms have also been proposed. For example, one may have a spectral difference between $p$ and He if their acceleration takes place in regions of different Mach numbers (Erlykin & Wolfendale 2015) due to the combination between time-dependent DSA (where the Mach number decreases with time) and a non-uniform He distribution in the medium (Ohira & Yoka 2011). Other authors proposed that a harder He spectrum may arise by preferential $\text{He}^{2+}$ injection occurring when the shock is stronger (Malkov et al. 2012). In Fisk & Gloeckler
(2012), it was proposed that elemental-dependent spectra may arise from acceleration in the interstellar space by a series of adiabatic compressions and expansions. From all these mechanisms, the $p/He$ ratio is expected to decrease steadily, as an intrinsic DSA property, up to the maximum rigidity attainable by the accelerators $R_{\text{max}} \sim 5$ PV.

Along with the $p/He$ anomaly, it is important to note that the single proton and He spectra are seen to experience a remarkable change in slope at rigidity above $\sim 100$ GV (Panov et al. 2009; Adriani et al. 2011; Yoon et al. 2011). Interpretations for this phenomenon fall in three classes (Vladimirov et al. 2012): acceleration mechanisms (Ptuskin et al. 2013), propagation effects (Tomassetti & Donato 2015; Thoudam & Horandel 2013; Bernard et al. 2013; Erlykin & Wolfendale 2012). The connection between the $p/He$ ratio anomaly and the spectral hardening of the single $p$ and $He$ fluxes is not obvious. Known explanations for the $p/He$ anomaly based on acceleration mechanisms do not automatically address this problem (Malkov et al. 2012; Serpico 2015), though it is said that concave spectra may arise from nonlinear DSA effects (Ptuskin et al. 2013) or from the time evolution of the Mach number at the shock (Ohira & Yoka 2011; Ohira et al. 2015; Erlykin & Wolfendale 2015). It is also believed that the absence of features in the $p/He$ ratio, in spite of the sharp structures of the individual $p$ and $He$ spectra, is suggestive of a common rigidity mechanism at the origin of the spectral hardening of both elements, either in acceleration or propagation (Adriani et al. 2014; Malkov et al. 2012; Blasi 2013).

In this Letter, we show that the $p/He$ anomaly and the spectral hardening in proton and He fluxes may be both signatures of the same physical effect, i.e., a flux transition between two source components characterized by different spectra and composition. The idea is that the $\sim$GeV–TeV component of the CR flux is ascribed to a hydrogen-rich source, presumably a nearby SNR characterized by a soft acceleration spectrum, while the multi-TeV flux is provided by the large-scale population of Galactic sources, namely, young SNRs with amplified magnetic fields and hard acceleration spectra. In this scenario, the “universality” of the acceleration spectra is not violated since each class of source is assumed to provide elemental-independent acceleration spectra. This work is motivated by the two following considerations on the CR spectrum that were not addressed in previous studies.

1. A high-energy flattening — despite the observed trend in the sub-TeV region, we note that the existing data at higher energies show no evidence of spectral differences between protons and He. The TeV band is experimentally accessible only by calorimetric measurements, with large systematic errors in the energy determination that may provoke large uncertainties in the slope or normalization of the fluxes. These errors are partially mitigated in the ratio between $p$ and $He$ in the energy region where they overlap. Figure 1 shows a compilation of $p/He$ data at multi-TeV energies. A power-law fit $E^\Delta$ between 1 and 200 TeV/nucleon gives $\Delta = 0.015 \pm 0.046$

2. A smooth spectral hardening — the AMS experiment has now measured with high precision the detailed variations of the proton and He spectra over three order of magnitude (Aguilar et al. 2015a,b). An important finding of the AMS collaboration is that the spectral hardening of CR hadrons is significantly smoother than that previously reported by PAMELA. In the PAMELA data, the spectrum was found to have a puzzling softening at rigidity $30–230$ GV followed by an abrupt spectral kink at $R \approx 230$ GV (Adriani et al. 2011). In contrast, the new AMS data show that the spectra of both species experience a progressive hardening at rigidity above $\sim 100$ GV (Aguilar et al. 2015a,b).

The hint of high-energy flattening for the $p/He$ ratio, if confirmed, would challenge the existing explanations of the anomaly in terms of intrinsic acceleration properties. In fact, from the proposed mechanisms, the steadily decreasing $p/He$ ratio would maintain its trend at multi-TeV energies. Also, the fact that the spectral hardening occurs gradually, without sharp structures, disfavors the usual argument that the $p/He$ ratio as function of rigidity cancels out the features on the proton and He spectra. From our perspective, the $p/He$ anomaly seems rather to be interpreted as the appearance of a broad feature at $R \sim 10–1000$ GV, asymptotically vanishing at higher rigidities, possibly connected with the progressive spectral variation of the two components. These considerations are suggestive of a common interpretation for the $p/He$ ratio and the single spectra hardening, as a natural feature arising from the presence of a nearby source component.

2. MODEL SETUP

We consider two classes of CR sources represented by a nearby SNR and the large-scale distribution of the Galactic SNR ensemble. The nearby source is associated with
the low-energy part of the flux and identified as an SNR at the latest stage of its evolution. At this stage, the magnetic turbulence can be substantially damped, and the shock is possibly weaker, so that softer acceleration spectra may be expected. On the other hand, for the Galactic ensemble component, it is expected that a large contribution to the flux comes from younger SNRs, with strong shocks, that efficiently accelerate CRs to multi-TeV energies. This association between flux components and source properties is motivated by our recent work in Tomassetti & Donato (2015), where we have shown that a two-component scenario is able to account for the positron fraction anomaly in terms of secondary production processes occurring in nearby SNRs, with observable consequences for primary/primary ratios between light and heavy elements (Tomassetti 2015b). For the aim of this work, the possible presence of hadronic interactions inside old SNRs is not strictly relevant. The source terms are modeled as $S_j^\nu(R) = Y_j \beta^{-1} (R/R_0)^{-\nu} e^{-R/R_{\text{max}}}$, according to the basic DSA mechanisms, where the constants $Y_j$ are the normalization factors for the $j$-type nuclei at the reference rigidity $R_0 \equiv 4 \text{ GV}$. The cutoff expresses the maximum rigidity attainable by the sources, taken as $R_{\text{max}} \equiv 5 \text{ PV}$. The spectral indices are taken as $\nu = 2.6$ for the nearby SNR component and $\nu = 2.1$ representing the Galactic ensemble. Contrary to our previous work, the indices $\nu$ are now taken as being elemental independent. The interstellar propagation is described using analytical calculations of CR diffusion and interactions (Tomassetti & Donato 2012). The diffusion region is modeled as a cylindrical halo, of half-thickness $L$, where the gas nuclei are distributed in a thin disk, of half-thickness $h$, with surface density $n_{\text{ism}} = 200 \text{ pc} \times 1 \text{ cm}^{-3}$. The diffusion coefficient is taken as spatially homogeneous, $K(R) = \beta K_0 (R/R_0)^3$, with $K_0/L = 0.1/5 \text{ kpc Myr}^{-1}$ and spectral index $\delta = 1/2$, for a Iroshnikov-Kraichnan spectrum of interstellar turbulence. With this setting, the B/C ratio is reproduced well. The diffusion equation is solved for all relevant CR nuclei after assuming stationarity, boundary conditions of zero density at $\pm L$, and continuity across the disk. For each $j$-type species, the equilibrium flux as function of energy is of the type $\phi_j = \frac{n_j}{\Delta E} L S_j/(L^2 + h^2 j_{\text{inel}}^\nu)$, where $j_{\text{inel}} = n \beta c \sigma j_{\text{inel}}^\nu$ is the destruction rate for collision in the ISM. The term $S_j^\nu j_{\text{tot}}$ represents the sum of the primary source terms, $S_j^{\nu pri}$, and a secondary contributions from the disintegration of heavier $k$-labeled nuclei, $S_j^{\nu sec} = \frac{\Delta E}{\Delta E_k} \sum_{k > j} \Gamma_{j \rightarrow k} \phi_j$. For $p$ and $\text{He}$, the secondary contribution is small but not completely negligible within the precision of the data. The nuclear reaction network is set up as in our previous studies. The heliospheric propagation is modeled under the force-field approximation, where the parameter $\Phi \equiv 800 \text{ MV}$ characterizes the strength of the modulation effect of the AMS observation period (Gleeson & Axford 1968).

3. RESULTS AND DISCUSSION

The model predictions for the proton and $\text{He}$ spectra are plotted in Fig. 2 as function of rigidity in comparison with the data. The proton flux $\phi_p$, tuned to reproduce the new AMS data, experiences a smooth spectral hardening at $R \gtrsim 100 \text{ GV}$ that is well described in terms of transition between the two components: the low-energy local source component $\phi_p^L$ (short-dashed lines) and the high-energy component of the Galactic ensemble $\phi_p^G$ (long-dashed lines). The AMS proton data are $\sim 3\%–4\%$ lower in normalization in comparison to the PAMELA data (Adriani et al. 2011). However, as reported recently (Adriani et al. 2014), a re-analysis of the PAMELA data determined a $3.2\%$ overestimation for the proton spectrum (and for the $p/\text{He}$ ratio). Thus, the results from the two experiments are consistent in normalization at the $\sim 1\%$ level. Discrepancies at low energies arise from the different modulation levels, which is partially mitigated in the $p/\text{He}$ ratio (Putze et al. 2011). For a closer inspection of the spectral variation, we compute differential spectral index $\gamma(R) \equiv d\log(\phi)/d\log(R)$. The functions $\gamma_p$ and $\gamma_{\text{He}}$ from the model are shown in Fig 3 in comparison with the new AMS data. The model describes very well the smooth evolution of the spectral index at in the $10–1000 \text{ GV}$ rigidity range. At higher rigidities, it can be seen that both species converge asymptotically to the same value, $\gamma^G \approx -\nu^G - \delta = -2.6$. 

![Fig. 2.](image1.png) 

**Fig. 2.** Top: rigidity spectra proton and helium multiplied by $R^{2.7}$. The solid lines indicate the model calculations. The flux contribution arising from the two components $\phi^L$ and $\phi^G$ are shown as dashed lines. The data are from and AMS (Aguilar et al. 2015a,b) and PAMELA (Adriani et al. 2011). 

![Fig. 3.](image2.png) 

**Fig. 3.** Proton and helium differential spectral index from the model in comparison with the data from PAMELA and AMS.
The p/He ratio is shown in the bottom panel of Fig. 2. In the model, the total p/He ratio (solid lines) is meant as the ratio $\phi_p/\phi_{He} \equiv (\phi_p^G + \phi_p^L)/\phi_{He}^G + \phi_{He}^L$. In the GV–TV range, the ratio falls off with rigidity in good agreement with the data. The model ratios for the single source components are also shown, i.e., $\phi_p^G/\phi_{He}^G$ (short-dashed lines) and $\phi_p^G/\phi_{He}^G$ (long-dashed lines). As shown, the p/He ratio associated to each source component is essentially flat above $\sim 10$ GV of rigidity, reflecting the universality of the acceleration spectra (i.e., the circumstance that each class of source provides composition-blind acceleration spectra). The GV-TV decreasing of the p/He ratio is therefore interpreted as a progressive flux transition between the low-energy region with ratio $\phi_p/\phi_{He} \sim \phi_p^L/\phi_{He}^L$, determined by the composition of the nearby source, and the high-energy region with $\phi_p/\phi_{He} \sim \phi_p^G/\phi_{He}^G$, dominated by the Galactic SNR ensemble. Remarkably, a combination of different source components with different composition may give a p/He ratio that is approximately power-law distributed in the $\sim 10–1000$ GV rigidity region. From the AMS data, the relative abundance at $R = R_0$ is found to be about 90% H and 10% He for the low-energy component, while the high-energy component has 82% H and 18% He. If the low-energy component is represented by a nearby SNR, such a localized source is subjected to composition variations with respect to the average elemental abundances of SNRs. Such variations may depend on the composition of the SN ejecta or on the circumstellar medium properties. A nearby source with hydrogen-rich background plasma may be suggestive of a remnant which is expanding over a molecular cloud, with relatively high medium density (Fujita et al. 2009; Kohri et al. 2015). In this case, the enhanced rate of proton-proton collisions occurring during DSA would explain the high-energy positron excess. One example is the Carina Nebula, where the absolute abundances of all $Z > 1$ elements are smaller than solar, unlike in an average SNR (Hamaguchi et al. 2007). SNRs with these properties have also been detected recently by the Fermi-LAT telescope, as discussed in Tomassetti (2015b). The idea that a local source might appear in the total CR spectrum is suggested by several studies (Malkov et al. 2012; Vladimirov et al. 2012; Moskalenko et al. 2003; Elykin & Wolfendale 2012) and supported by independent observations (Benitez et al. 2002). For a source placed within distance $d \sim 500$ pc, the maximum flux would be detected after time $\tau \sim d^2/K$ that is of the order of Myr, in the GV-TV rigidity range, from the parameters adopted for $K(R)$. An SN explosion occurred a few Myr time ago may supply the observed flux if a total energy $E_{CR} \sim 10^{50}$ erg is released into CRs. A detailed and interesting study on the local source properties is found in a very recent work in Kachelrieß et al. (2015), where a similar scenario is proposed (and supported by a trajectory calculation approach). Furthermore, similar signatures are also expected in other primary/primary ratios, as variations in metal abundance are likely. A high-energy flattening, however, is unavoidable under this scenario. As shown in Fig. 4, the p/He ratio is predicted to level off at the value $p/He \sim 8$, which is remarkably consistent with the value obtained from the multi-TeV power-law fit of Fig. 1. As discussed, the p/He flattening is supported by the existing data, but the situation in not sufficiently clear. The new AMS data, for instance, are compatible with a single power law up to 1.8 TeV of energy. It should also be noted that, in this calculation, we employed $R_{max} \approx 5$ PV for both components. As discussed in previous studies (Tomassetti & Donato 2015), the local component may have limited energy in the 1–10 TV range, as is common for old SNRs where the magnetic field amplification is no longer effective. This parameter is therefore important in modeling the secondary production of $e^\pm$ pairs. Concerning the p/He ratio, a better clarification may come soon with data at the higher energy expected from the ISS-CREAM experiment (See et al. 2014), to be launched very soon, or the CALET payload (Adriani et al. 2014), which has been now installed on the ISS and successfully activated (Maestro 2015).  

4. CONCLUSIONS

This work is motivated by the search for a comprehensive model of Galactic CRs that is able to account for the several intriguing anomalies recently observed in their spectrum. The need for local sources is established at least in the leptonic channels, thanks to new AMS data. A possible connection between leptonic and hadronic anomalies is proposed in Tomassetti & Donato (2015), with the presence of a local and old SNR contribution in the GeV–TeV spectrum. As discussed, such a two-component scenario loses one distinctive feature of hadronic models for the CR positron excess, i.e., the high-energy rise in secondary/primary nuclear ratios (which is not observed). On the other hand, we have shown that new signatures can be found in primary/primary ratios. Calculations of light/heavy nuclear ratios were reported in Tomassetti (2015b). In this Letter, focused on the p/He anomaly, we have argued that composition variations in the local SNR may provoke the appearance of broad spectral features at $\sim 10–1000$ GeV energies that can be misinterpreted as an apparent violation of universality. In summary, we have shown that a large variety of spectral anomalies can be explained under a simple two-component picture. It now remains to be understood how likely the emergence of individual sources in the CR spectrum is. Further elaborations are being carried out beyond the steady-state
approximation in order to account for the stochastic nature of SNR events and their actual relevance on the local CR flux. As argued in Tomassetti (2015b), this approach is important for modeling the diffusive γ-ray emission in other parts of the Galaxy, which may in general be influenced by CR flux components injected from individual SNRs. Observationally, upcoming AMS data on secondary nuclei will be of great importance for discriminating among different propagation models. For instance, the detection of a high-energy flattening in the B/C or Li/C ratio (possibly consistent with a corresponding $\bar{p}/p$ flattening) would probably disfavor the scenario proposed here (Serpico 2015).

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